Basic Comparison Of Fix Capacitor-Thyristor Controlled Reactor, FC-TCR (SVC) And Thyristor Controlled Series Capacitor (TCSC) In Electric Power System

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Abstract: In this work, effort is concentrated on explicit exposure of similarities and differences between FC-TCR and TCSC devices in electric system. Several distinct and common operational features of the two components are addressed and evaluated to build a comprehensive analysis for adequate comparison and contrast of the FACTS controllers. The two different models of the devices that split up their identically composed adjustable parameters (in terms of constituting components) into $B_{SVC}$ and $X_{TCSC}$ are clearly demonstrated in attempt to ex-ray the relative functionalities of the controllers in power system. All the diagrams are very illustrative in picturing out the structural composition of FC-TCR and TCSC equipments in order to point at the obvious similitude of their basic circuit. Apart from the self-explanatory and theoretical preamble that leads the introduction, the nature of the work takes a posture of two-way stance in which the similar and varied characteristics of the controllers are vertically featured; thereby, covering the structural, functional and “installational” comparison; all displayed in a tabular form.

Keywords: Comparison, TCSC, FC-TCR, Electric, System

I. INTRODUCTION

FACTS equipments by IEEE recommendation are categorized into series, shunt and combined series-shunt controllers. Among the series elements of the FACTS family include thyristor controlled series capacitor (TCSC), static synchronous series compensator (SSC) etc.

The series reactance of power lines can be improved upon to meet the system requirement in attempt to enhance the active power flow on the line. In this case; the existing branch voltages are coupled in series with the line so as to achieve optimum power transfer. Similarly, improvement of bus voltages is often by automatic amendment of susceptance of installed shunt component on the bus.

In some cases, direct effect of the improved voltage magnitudes on the network buses stems from the impact of bus connected FACTS components such as shunt controllers – SVC, STATCOM etc and this influence is not monopolized by the connecting bus areas only; but can be far reaching to other neighboring buses, depending on the reactive power compensation capability of the shunt controllers in question. This augments system voltages in order to eliminate bus voltage deficit.

In a true network operation where the system’s high operational efficiency is in great demand, it is seldom having a situation where only a single controller functions to achieve all the network requirements. As a result; agglomeration of the functional input of the three categories is always experienced in order to benefit from the independent properties of each of the FACTS controller family.

Also, Integration of the series and shunt FACTS controllers into a single component for efficient operation of power system can be appropriated from the combination of the two devices out of the two independent categories to form composite equipment known as shunt-series controller. In effect, separate inherent functional characteristics of each of
the constituent members is being harnessed to achieve a better performance that may not be completely offered by one alone, when operating independently from the other in the system. As a result, unified power flow controller (UPFC) can control a host number of system situations in accordance to the behavior of individual constituents of the unit. This is more preferable considering cost implication; especially, when embarking on a large scale system improvement planning.

In summary, there is always integration of the functional potency of the three classes in the light of accomplished optimum equipment localization within the network; and this to a larger extent helps to induce a high degree of steady and dynamic stability of the power system; thus, establishing a rugged and efficient electrical environment through the system operation under a well electrically instituted conditions such as

✓ Proper sub-synchronous resonance (SSR) control
✓ A constant electrical fault-free condition
✓ Effective power flow control as well as
✓ Adequate power oscillation damping within the power system.

FACTS equipment has been defined by IEEE as “AC” transmission system incorporating power electronic based and other static controllers to enhance controllability and increase power transfer. Inclusion of power electronics as the basic components of the equipments suggests the key functional entity of the devices and this is glaring from the control concept of the system. As such, thyristor devices have immensely contributed to the success in usage of FACTS controllers, since, the adjustment of the network constants to implement the desired system objectives is necessitated by the power electronic composition. Through a firing and appropriately timed pulses, the right firing angle, α , can be decided for triggering on and off, the thyristor switches. This is done on a considerable level of precautions to avoid operating within the resonance angle, α_{res} and the tendency for system oscillation.

SECTION 1

MODELING OF STATIC VAR COMPENSATOR (SVC) AND THYRISTOR CONTROLLED SERIES CAPACITOR.

THYRISTOR CONTROLLED SERIES CAPACITOR MODEL

The equivalent reactance of the system that is connected with TCSC is the summation of adjustable TCSC reactance, X_{TCSC} and the natural reactance of the system lines, X itself. Among the components of line reactance are the line charging capacitance and inductance, neglecting the line resistance. Therefore, for a system with installed TCSC component, the equivalent line reactance of the network is as stated below

\[ X_{eq} = X_{Line} + X_{TCSC} \] ...

\[ X_{TCSC} = \frac{x_c}{X + x_c} \]

\[ X_{eq} = X_{Line} + \frac{x_c}{X + x_c} \cdot \frac{|X_{Line} (x_c + x_L) + x_c x_L|}{X + x_c} \]

Taking, \( X_L = \alpha L \) and \( X_C = 1/\omega C \)

By substitution,

\[ = \left( X_{Line} \left( \frac{1}{\omega C} + \frac{1}{\omega L} \right) + \frac{1}{\omega C} - \frac{1}{\omega L} \right)^{-1} \]

\[ = \left( X_{line} \left( \frac{\omega^2 L C + 1}{\omega} \right) + \frac{1}{\omega C} \left( \frac{\omega^2 L C + 1}{\omega} \right)^{-1} \right) \]

Where, \( X_{equ} = \) Equivalent or total reactance on the system.

\[ X_{Line} = \text{natural line reactance of the system} \]

\[ I_l (\alpha)(s) = I_0 B [\sin \alpha - \frac{\omega}{\omega_0} \sin \omega_0] \] ...

From the basic circuit of figure 1 above, the thyristors of the circuit decide the level of participation of capacitor component for line compensation. The capacitor can be completely bypassed when the thyristor switches are fired at a suitable angle, \( \alpha \) ; then, allowing line current to pass through inductor branch and resulting such expressions as

\[ I_l (\alpha)(s) = I_0 B [\sin \omega t - \frac{\omega}{\omega_0} \sin \omega_0] \] ...

(for inductor current)

Full capacitive compensation occurs when SW \(_1\) and SW \(_2\) thyristor are switched off as shown, permitting the current flow through capacitor C only. See the diagram below.

Figure 1.1: Diagram showing line series circuit with thyristor component switched off

Therefore; the quantity of current that are allowed to pass through the capacitor determines the extent of charging and discharging of C and the development of voltage magnitude which is in quadrature with the line current and in series with the line. The voltage expression is as shown below

\[ V_C(t) = I_0 X_C \cos \omega t \] ...

This largely account for the system reactive power compensation as obtained with thyristor controlled series capacitor (TCSC).

The figure below shows the graph of the equivalent reactance, \( X_{eq} \) plotted against the thyristor firing angle, \( \alpha \).
The positive half with the curve extending from $X_{\text{bypass}}$ ($\alpha = 0$), sweeping across the plane towards the resonance shows the inductive region. The firing angles that are traceable to this curve are the range of angles within which inductive compensation is attainable, with $X_{\text{MAX}}$ being the maximum attainable equivalent reactance.

The effectiveness of the equivalent reactance, $X_{\text{eq}}$ for TCSC is limited at the resonance point where $\alpha = \alpha_{\text{res}}$, and for normal operations, the firing angle must be maintained at a particular length, $\Delta \alpha$ away from the resonance angles $\alpha_{\text{res}}$. This gives room for maximum and minimum reactance (i.e. $X_{\text{MAX}}$ and $X_{\text{MIN}}$) corresponding to the upper and lower bound of $X_{\text{eq}}$ axis respectively. From the graph, at $\alpha = 0$, there is a continuous triggering of the thyristor switches. Thus, the basic circuit behaves as a parallel connected L C circuit. This is known as bypass mode. When $0^0 < \alpha < \alpha_{\text{res}}$, the angle ranges below the resonance angle, $\alpha_{\text{res}}$ but greater than $0^0$; and at this range, the equivalent reactance, $X_{\text{eq}}$ is positive and inductive. This is referred as inductive boost mode.

In capacitive boost mode, angle $\alpha$ is greater than resonance angle, $\alpha_{\text{res}}$ but lesser than $90^0$ (i.e. $0^0 < \alpha < 90^0$). As such the equivalent reactance is negative and capacitive in nature. Subsequently, as the firing angle equals $90^0$ ($\alpha = 90^0$), the thyristor is no more conductive and triggerable. As result, the effect of the fixed capacitor is largely felt on the line and this is called blocking mode.

For static Var Compensator, the adjustment of line parameters is by maneuvering the inductive susceptance of the device, $B_{L(\alpha)}$ which is controllable through the thyristor firing angle to determine the branch current. It is worth knowing that capacitor $C$ is fixed in value and can allow capacitive current into the line depending on $SW_1$ and $SW_2$ switching mode. The expression that relates the inductive and capacitive reactance in the circuit can be derived thus:

$$L_\text{VC} \cdot C = B_{L(\alpha)}$$

II. STATIC VAR COMPENSATOR MODELING

In this modeling, a FC-TCR basic circuit which is the same in component composition with the TCSC counterpart is presented; though with absolute incongruity in terms of direction and area of installation in power system, as we can observe comparing the two modeling. As shown below, unlike TCSC equipment; the device occupies the bus through a protective circuit breaker and a shunt transformer to emerge a typical variable susceptance, $B_{\text{SV}}$ assumed as the element of reactive power control for bus voltage improvement. The equivalent susceptance of the device, $B_{\text{eq}}$ comprises of thyristor-dependent adjustable inductive susceptance, $B_{L(\alpha)}$ and a fixed capacitive, susceptance, $B_C$; all mathematically related with the natural constituent variables as shown in the equations.
Therefore, the upper and lower bound (i.e. $B_{SVC(lower)}$ and $B_{SVC(upper)}$) in the graph result the total susceptance which is a function of inductive and capacitive susceptance as expressed above.

From equation (4), the firing angle, $\alpha$ shows the variability of the equivalent susceptance through the two connected thyristor devices. Taking $B_{eq}$ as a susceptance for SVC of a certain bus k and the associated active power at the same bus to be $O$, the corresponding power flow equation can be expressed as follow:

$$Q_{SVC} = -V_k^2 B_{SVC}$$

The expression of equation (6) shows the reactive power, $Q_{SVC}$ as a function of square of bus voltage, $V_k$ and the susceptance, $B_{SVC}$ at bus k. Reactive power demand variation requires a corresponding adjustment of susceptance connected to bus K. This is to eliminate reactive power deficit; thus increasing the supply so as to maintain the bus voltage at the system required level.

![Diagram showing the graphical illustration of the dependency of thyristor firing angle on the FC-TCR equivalent susceptance](image1.png)

**Figure 1.4:** Diagram showing the graphical illustration of the dependency of thyristor firing angle on the FC-TCR equivalent susceptance.

<table>
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<th>STRUCTURAL SIMILARITIES</th>
<th>TCSC</th>
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<td>1. Presence of TCR branch for Reactive power control</td>
<td>TCR branch is also present for thyristor control action</td>
<td>Power system line compensation is accomplishable in series connection of TCSC with the line in order to improve series line voltages for system stability</td>
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<tr>
<td>2. Availability of capacitor device for reactive power injection</td>
<td>Also, capacitor is available for improvement of line series compensation</td>
<td>Enhancement of system power potential is attainable being that the system line series voltage is efficiently augmented to give a conducive room for optimum power transportation in the face of system dynamic and steady state conditions.</td>
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<tr>
<td>3. The basic circuit comprises of thyristors in opposite direction of connection, reactor element and a bank of fixed capacitor</td>
<td>The basic circuit consists of the same bank of capacitor, a reactor element, two thyristor components connected in opposite direction to each other</td>
<td>Similarly, generation of thyristor control mechanism for power flow regulation</td>
</tr>
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<td></td>
<td></td>
<td>Possibly of adopting thyristor control mechanism for power flow regulation</td>
</tr>
<tr>
<td><strong>Basic circuit diagram of an FC-TCR device</strong></td>
<td><strong>Basic circuit diagram of a TCSC device (the same with FC-TCR device)</strong></td>
<td><strong>TCSC can equally be controlled using PI control system.</strong></td>
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<td><strong>The same basic PI control System schematic diagram as with TCSC device</strong></td>
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<td><strong>TCSC also effects line compensation through power system parameter adjustment.</strong></td>
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<tr>
<td>4. Possibility of control through thyristor firing angles for system bus voltage regulation</td>
<td>The same basic PI control System schematic diagram as with TCSC device</td>
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<td>5. Controllable via the PI control Unit</td>
<td>6.FC-TCR adjusts system parameters, in attempt, to effect reactive power compensation</td>
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<td></td>
<td>There is no obvious structural dissimilarity in terms of component composition between thyristor controlled series capacitor(TCSC) and fix-capacitor thyristor controlled reactor (FC-TCR) except in the area of the equipments installation within the power system; in which the incorporation of shunt transformer with FC-TCR creates a remarkable compositional installation difference between the two FACTS equipments. In exception of these, the two controllers are structurally</td>
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equivalent, apart from in minor situations where inclusion of some accessorional equipments are done on the basis of achievement of a desired purpose such as in harmonic control. Etc

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<tr>
<td>1. Fundamentally, the chief functional behavior of FC-TCR devices in electric system is to upgrade the system bus voltages so as to enhance stability.</td>
<td>The apparent and distinguishing operational activities of a TCSC in electric system is in improvement of electric power flow through line series voltage supplement.</td>
<td>Variation of thyristor control angles into the resonance, ( \alpha_{res} ) does not cause problem when the thyristor angles are manipulated for susceptance adjustment.</td>
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<tr>
<td>2. For FC-TCR and other devices in SVC family, resonance angle, ( \alpha_{res} ) does not cause problem when the thyristor angles are manipulated for susceptance adjustment.</td>
<td>Variation of thyristor control angles into the resonance, ( \alpha_{res} ) results power oscillatory problem. For that a short angular distant, ( \Delta \alpha ) is usually maintained within the inductive plane to avoid power system oscillation while varing the angle.</td>
<td>The range of thyristor firing angle variation mathematically exists within ( 90^0 \leq \alpha \geq 180^0 ) for adequate compensation function.</td>
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<td>3. The range of firing angle variation mathematically exists within ( 90^0 \leq \alpha \geq 180^0 ) for adequate compensation function.</td>
<td>The variable reactance equation is the inverse of that of TCSC:</td>
<td>The range of thyristor firing angle variation mathematically obtained within ( 0^0 \leq \alpha \geq 90^0 ) for effective compensation.</td>
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<td>4. Variable reactance equation is inverse of that of TCSC:</td>
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<tr>
<td>( 1/X_{eq} = \frac{\omega_0^2}{L_0 C_0} \cdot \frac{\alpha_{res} - \alpha}{\alpha_{res} - \alpha_{res}} ) [ \omega_0 ] [ \alpha_{res} ] [ \alpha_{res} ]</td>
<td>( X_{tscs} = \frac{\alpha_{res} \cdot \omega_0}{\omega_0 L_0 C_0} - 2 \cdot \frac{\alpha_{res} \cdot \omega_0}{\omega_0 L_0 C_0} )</td>
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<td>5. The PI control output for FC-TCR is ( B_{SVC} ).</td>
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<tr>
<td>6. FC-TCR is installed in shunt with the system bus.</td>
<td>The TCSC is installed in series with transmission lines.</td>
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III. CONCLUSION

It is important to note that the two devices share the same structure just as briefly explained in the comparison table since the component composition of the two equipments are common. In the case of functional behavior and characteristics in terms of steady state condition evaluation; the two are obviously related considering the reactance of the TCR fragment which is the major points of similarity of the two; visa-vise, the operational effect on the system.

With FC-TCR and other family members of static Var compensators, SVC; if the device is at the system bus voltage location and the operating voltage on the FACT elements is the bus voltage and a sinusoid; a furrier analytical evaluation with respect to reactor current waveform gives a clear view of TCR reactance at fundamental frequency to be similar with adjustable reactance expressed as

\[
X_{adj.} = \frac{X_L}{2(\pi - \alpha) + \sin 2\alpha} \tag{8}
\]

\[
X_{adj.} = \frac{2\pi fL}{2(\pi - \alpha) + \sin 2\alpha} \tag{9}
\]

Thus, the equation can be further expanded to incorporate the capacitive and inductive reactance ratio in the overall effective reactance as shown below:

\[
X_{eff}(\alpha) = \frac{X_C \cdot \pi \cdot \sin 2\alpha}{(X_L/X_C)} \tag{10}
\]

\[
X_{eff}(\alpha) = \frac{(X_C^2 \cdot \sin 2\alpha)/(2\pi)}{2(\pi - \alpha) + \sin 2\alpha} \tag{11}
\]

Where,

\[
2\pi fL = X_L, \quad \text{the inductive reactance of the reactor at fundamental frequency. \quad 1/2\pi f C = X_C, \quad \text{the capacitive reactance of the capacitor at fundamental frequency.}
\]

\[
\alpha = \text{thyristor firing angle}
\]

\[
f = \text{system fundamental frequency}
\]

\[
l = \text{inductance of the reactor of the device}
\]

\[
C = \text{the device capacitor}
\]

The extent of the equipment functional participation is the decision of the thyristor firing angle whose range of variation is predetermined at the manufacturing stage. Adjustment of the controller through the angle enables the effective reactance variation so as to determine the degree of bus voltage changes assuming the basic circuit is connected in shunt with the bus.

Functionally FC-TCR is always installed on the bus through a step down transformer; (unlike TCSC device that occupies the line in series order) on the high voltage or extra-high voltage side as the case may demand so as to reduce the device voltage to such a bearable capacity as 50kv and below.

From the derived expression, the apparent similarity of FC-TCR reactance with TCSC reactance is very clear. It is inevitably imperative to know that the basic circuit is truly the same as well as their reactance when looking at the structure and component make-up; but differ in terms of function and position since the two devices do not maintain the same direction when connected on the system for reactive power provision. While the circuit is installed in series in a system for TCSC device to maintain the adjustable reactance \( X_{adj.} \) or \( X_{eff}(\alpha) \) as the case may be) on the line; the same basic circuit maintains shunt position changing from series reactance to susceptance due to parallel/shunt position on the system bus; thereby, establishing a clearly drawn demarcating

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line for distinction between the two devices. In the mode as seen above, the equivalent circuit can conveniently serve a major purpose of real power flow enhancement in assumption of series position with the line. Thus; voltage incorporated from the circuit, complements the natural series line voltage of the system to reinforce the network power transfer potential.

On the other hand; the TCSC adjustable series reactance ($X_{adj}$ or $X_{eff}(\alpha)$) automatically changes to FC-TCR adjustable susceptance ($\frac{1}{X_{eff}(\alpha)} = B_{eff}(\alpha)$ or $\frac{1}{X_{adj}} = B_{adj}$) when connected in shunt to bus for exchange of reactive power with the system in other to regulate bus voltages.

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