

Effect Of Normalization Techniques In Robot Selection Using Weighted Aggregated Sum Product Assessment

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Abstract: The process of Selecting Industrial Robot from number of alternatives having advanced features is a complex and tough job. This choice of selecting the best out of all the available alternatives can be done with the help of Multi attribute Decision making (MADM) Methods. The main focus of this paper is to select an industrial robot using weighted aggregated sum product assessment method (WASPAS) using best normalization technique. Normalization is the first step which makes the decision matrix comparable. The raking performance was compared with other MADM method for the same example with the help of Spearman's rank correlation coefficient. The effect in the raking order was studied for normalization technique. Linear Normalization (Max-Min) proved to be best normalization method for WASPAS.

Keywords: WASPAS, MADM, Normalization, Robot selection

I. INTRODUCTION

Industrial robotic manipulators are general purpose machine to do certain task like moving materials, tools or parts. There are other reprogrammable robots which can be used for welding, spray painting and do certain hazardous task. Robots perform these tasks with precision, accuracy and can also increase the productivity. In today's competitive world a large number of robots are available in the market with different specification. While selecting a robot the decision maker should look in detail all the attributes which affect the manipulators performance. The attributes can be categorized into beneficial and non beneficial attributes. The attributes in which higher value is desired are known as beneficial attributes like load carrying capacity, end effectors reach etc. Attributes in which lower value is desired is termed as non beneficial attributes like cost, error etc. All these attributes have different unit and are conflicting in nature. Thus decision makers face difficulty in comparing different attributes and selecting Robot.

Researchers have solved various industrial robot selection problems using MADM methods. Also the effect of normalization methods was checked on these MADM methods. This paper is another attempt to check the variation in raking performance with the change in normalization technique in a new MADM method i.e. WASPAS method. This paper contain seven section introduction, the literature review of the previous work, Normalization Techniques employed in the paper, Weighted Aggregated Sum Product Assessment method, its application with the help of Illustrative Example, Comparative Analysis with other methods and conclusion.

II. LITERATURE REVIEW

Agrawal et al. (1991) using Technique for Order Preference by Similarity to Ideal Solution (TOPSIS) method created a rank for the selection of industrial robots. Jian Ma (1999) proposes an approach to find weights of attribute in the

MADM problems. A Robot selection example was considered to illustrate the suitability of the approach. Pavličić, D. (2001) checked the effect of normalization in MADM methods like SAW, TOPSIS and ELECTRE. Bhangale et al. (2004) used graphical methods and TOPSIS for the selection of industrial robot. He evaluated and compared the relative rankings of the robots which were derived using the above mentioned methods. Rao, and Padmanabhan (2006) Presented digraph and matrix method for the selection of industrial robots. A robot selection index was created which ranked the robots for industrial application. Rao and Padmanabhan (2007) presented digraph and matrix method for the selection of industrial robots. A robot selection index was created which ranked the robots for particular industrial application. Rao (2007) has compared different MADM methods for the selection of Industrial robot and other manufacturing method. Chakraborty, S., & Yeh, C. H. (2007) in his simulation study proved that vector and linear scale transformation, method are best for SAW. Zavadskas, E. K., & Turskis, Z. (2008) introduced a new logarithmic normalization technique for MADM methods. Devi (2011) extended VIKOR method in intuitionistic fuzzy environment, aimed to solve MADM problems. The weights of alternatives were taken as triangular intuitionistic fuzzy set. A robot selection problem for material handling was used to verify the proposed method. Athawale and Chakraborty (2011) compared the ranking performance of ten Multi Criteria Decision Making methods used for the selection of robots engaged in industrial activities. Singh and Rao (2011) proposed a hybrid of graph theory and matrix approach (GTMA) along with analytical hierarchy process (AHP). The potential of method was checked and compared with other methods. Šaparauskas et al. (2011) and Zavadskas et al. (2013) considered three criteria of optimality for ranking the facades of commercial and public building using Weighted Sum Model (WSM), Weighted Product Model (WPM) and WASPAS. These were compared with Multiple Objective Optimization on the basis of Ratio Analysis (MOORA) method. Athawale et al. (2012) applied compromise ranking method for selecting Industrial Robot. Mondal and Chakraborty (2013) compared models of data envelopment analysis (DEA) to identify robots having optimum performance in order to satisfy the objectives with respect to cost and other parameters. Chakraborty and Zavadskas (2014) solved eight manufacturing decision making problems. It was found that WASPAS has the ability of ranking accurately the alternatives in all the eight selection problems. Azimi et al. (2014) presented Polygons Area Method for robot selection problem. The results obtained were compared with the result of other MADM methods using Spearman's rank correlation coefficient. Chatterjee, P., & Chakraborty, S. (2014) checked the effect of normalization in PROMETHEE, grey relation analysis (GRA) and TOPSIS for flexible manufacturing system selection. Çelen, A. (2014) evaluated the normalization effect on TOPSIS method for financial performances of 13 Turkish banks. Chakraborty and Antucheviciene (2015) illustrated the acceptability of WASPAS as a multi attribute decision making tool using five real time manufacturing related problems. Jahan, A., & Edwards, K. L. (2015) investigated the influence of normalization techniques in ranking performance of MADM methods. Vafaei, N. et al.

(2016) investigated the normalization effect on Analytical Hierarchy Process (AHP). Karande, P. et. al. (2016) in his paper compared the ranking performance of 6 MCDM methods. It was found that the multiplicative form of MOORA is least affected by the change of weights.

III. NORMALIZATION TECHNIQUES

$X = [x_{ij}]_{m \times n}$ is the Decision matrix, where x_{ij} is the performance value of i^{th} alternative and j^{th} attribute, m is the number of available alternatives and n is the number of attributes. The performance is made dimensionless and comparable with the help of normalization. This is one of the important steps in solving decision making problem. \bar{X}_{ij} is the normalized value of X_{ij} . The different normalization techniques used in this paper is presented in Table 1.

S. No.	Normalization technique	Condition of use	Formula
N1	Vector Normalization Jahan, A., & Edwards, K. L. (2015)	beneficial	$\bar{X}_{ij} = \frac{X_{ij}}{\sqrt{\sum_{i=1}^m X_{ij}^2}}$
		non beneficial	$\bar{X}_{ij} = 1 - \frac{X_{ij}}{\sqrt{\sum_{i=1}^m X_{ij}^2}}$
N2	Linear Normalization (Max) Çelen, A. (2014)	beneficial	$\bar{X}_{ij} = \frac{X_{ij}}{X_j^{Max}}$
		non beneficial	$\bar{X}_{ij} = 1 - \frac{X_{ij}}{X_j^{Max}}$
N3	Linear Normalization (Max-Min) Çelen, A. (2014)	beneficial	$\bar{X}_{ij} = \frac{X_{ij} - X_j^{min}}{X_j^{Max} - X_j^{min}}$
		non beneficial	$\bar{X}_{ij} = \frac{X_j^{Max} - X_{ij}}{X_j^{Max} - X_j^{min}}$
N4	Linear Normalization (Sum) Çelen, A. (2014)	beneficial	$\bar{X}_{ij} = \frac{X_{ij}}{\sum_{i=1}^m X_{ij}}$
		non beneficial	$\bar{X}_{ij} = \frac{1/X_{ij}}{\sum_{i=1}^m (1/X_{ij})}$
N5	Logarithmic Normalization Jahan, A., & Edwards, K. L. (2015)	beneficial	$\bar{X}_{ij} = \frac{\ln X_{ij}}{\ln(\prod_{i=1}^m X_{ij})}$
		non beneficial	$\bar{X}_{ij} = \frac{1 - \ln X_{ij}}{m - 1 - \ln(\prod_{i=1}^m X_{ij})}$
N6	Enhanced accuracy Normalization Jahan, A., & Edwards, K. L. (2015)	beneficial	$\bar{X}_{ij} = 1 - \frac{X_j^{Max} - X_{ij}}{\sum_{i=1}^m (X_j^{Max} - X_{ij})}$
		non beneficial	$\bar{X}_{ij} = 1 - \frac{X_{ij} - X_j^{min}}{\sum_{i=1}^m (X_{ij} - X_j^{min})}$

Table 1: Different normalization techniques

IV. WASPAS METHOD

Weighted sum model (WSM) and weighted product model (WPM) are combined to create a new MADM model

i.e. Weighted Aggregated Sum Product Assessment Method (Chakraborty and Zavadskas 2014). The joint criterion of optimality is obtained by weighted summation of two criteria of optimality. The 1st criterion of optimality is similar to that of Weighted Sum Model. The total relative importance of the alternatives are calculated with the help of equation (1)

$$Q_i^{(1)} = \sum_{j=1}^n \bar{X}_{ij} W_j \quad (1)$$

W_j are weights associated/ allocated to j^{th} attributes

Then the second criterion of optimality is similar to Weighted Product Model. The relative importance of the alternative are calculated with the help of equation (2)

$$Q_i^{(2)} = \prod_{j=1}^n (\bar{X}_{ij})^{W_j} \quad (2)$$

A joint generalized criterion of weighted aggregation of additive and multiplicative methods is then proposed as follows (Zavadskas et al., 2013)

$$Q_i = 0.5Q_i^{(1)} + 0.5Q_i^{(2)} = 0.5 \sum_{j=1}^n \bar{X}_{ij} W_j + 0.5 \prod_{j=1}^n (\bar{X}_{ij})^{W_j} \quad (3)$$

V. ILLUSTRATIVE EXAMPLE

To validate and check the accuracy of WASPAS method with different normalization methods, an example is considered which deals with the selection of the industrial pick-n-place robot. Bhangale et al. (2004) created a preference list for robots using graphical methods and TOPSIS. The criteria on which industrial robot are selected is specified as attributes of the robot. These attributes can be categorized as beneficial and non beneficial. The beneficial attributes in this example are Load carrying capacity, memory capacity (MC), maximum tip speed (MTS) and manipulator reach (MR). Repeatability error (RE) is a non beneficial attribute. Rao (2007) determined the weights of the attributes using AHP method, WLC = 0.036, WRE = 0.192, WMTS = 0.326, WMC = 0.326 and WMR = 0.12, which will be used for subsequent analyses.

Weights of Attributes →		0.036	0.192	0.326	0.326	0.12
S. No.	Robot	LC (kg)	RE (mm)	MTS (mm/s)	MC	MR (mm)
1	ASEA-IRB 60/2	60	0.4	2540	500	990
2	Cincinnati Milacrone T3-726	6.35	0.15	1016	3000	1041
3	Cybotech V15 Electric Robot	6.8	0.1	1727.2	1500	1676
4	Hitachi America Process Robot	10	0.2	1000	2000	965
5	Unimation PUMA 500/600	2.5	0.1	560	500	915
6	United States Robots Maker 110	4.5	0.08	1016	350	508
7	Yaskawa Electric Motoman L3C	3	0.1	177	1000	920

Table 2: Decision Matrix for Robot Selection Bhangale et al. (2004)

The Decision matrix is normalized using various normalization techniques. Table 2 shows the decision matrix for robot selection by Bhangale et al. (2004). The decision matrix is vector normalized, final value of

Q_i^1, Q_i^2 and joint generalized criteria for WASPAS " Q_i " was calculated which is shown in Table 3. It can be seen that the ranking performance of the vector normalized WAPAS is 3-2-4-1-6-5-7. Similarly the generalized criterion of WASPAS and ranking was calculated using various normalization techniques shown in Table 4. Where N1, N2,....., N6 are the serial number corresponding to normalization technique as shown in Table 1. $Q_i^{N1}, Q_i^{N2}, \dots, Q_i^{N6}$ are the performance criteria of WASPAS using normalization technique N1,N2,.....,N6 respectively.

S. No	Robot	LC (kg)	RE (mm)	MTS (mm/s)	MC	MR (mm)	Q_i^1	Q_i^2	Q_i
1	ASEA-IRB 60/2	0.9705	0.2138	0.7087	0.1217	0.3557	0.3894	0.2952	0.3423 (4)
2	Cincinnati Milacrone T3-726	0.1027	0.7052	0.2834	0.7303	0.374	0.5145	0.4582	0.4863 (2)
3	Cybotech V15 Electric Robot	0.1099	0.8034	0.4819	0.3651	0.6022	0.5066	0.473	0.4898 (1)
4	Hitachi America Process Robot	0.1617	0.6069	0.2790	0.4869	0.3467	0.4137	0.3909	0.4022 (3)
5	Unimation PUMA 500/600	0.04043	0.8034	0.1562	0.1217	0.3288	0.2858	0.2054	0.2456 (6)
6	United States Robots Maker 110	0.07278	0.8427	0.2834	0.0852	0.1825	0.3065	0.2133	0.2599 (5)
7	Yaskawa Electric Motoman L3C	0.04852	0.8034	0.0493	0.2434	0.3306	0.2911	0.1782	0.2346 (7)

Table 3: Vector normalized decision Matrix

S. No.	Robot	Q_i^{N1}	Q_i^{N2}	Q_i^{N3}	Q_i^{N4}	Q_i^{N5}	Q_i^{N6}
1	ASEA-IRB 60/2	0.342317 (4)	0.243608 (7)	0.214987 (4)	0.142556 (4)	0.152538 (1)	0.792384 (7)
2	Cincinnati Milacrone T3-726	0.486362 (2)	0.622574 (2)	0.605407 (2)	0.183018 (2)	0.151381 (2)	0.902112 (2)
3	Cybotech V15 Electric Robot	0.489813 (1)	0.634132 (1)	0.627671 (1)	0.188539 (1)	0.150857 (3)	0.919419 (1)
4	Hitachi America Process Robot	0.402278 (3)	0.506704 (3)	0.474559 (3)	0.147004 (3)	0.150295 (4)	0.857 (3)
5	Unimation PUMA 500/600	0.245609 (6)	0.302272 (5)	0.146553 (7)	0.086335 (6)	0.13114 (6)	0.833053 (6)
6	United States Robots Maker 110	0.259917 (5)	0.319789 (4)	0.1545 (5)	0.096957 (5)	0.13263 (5)	0.840142 (4)
7	Yaskawa Electric Motoman L3C	0.234661 (7)	0.287461 (6)	0.151302 (6)	0.082541 (7)	0.128212 (7)	0.833526 (5)

Table 4: Generalized criteria of WASPAS and ranking obtained from normalization techniques

VI. COMPARATIVE ANALYSIS

To check the effect on ranking performance of WASPAS method with different normalization technique, their ranking performance was compared with other MADM methods cited in Table 5. Karande, P. et al. calculated the ranking for same example using the same weight using different MADM method, ranks obtained from Ratio system method was 5-1-2-4-7-6-3 and from reference point method was 5-2-1-3-5-7-4. This was done with the help of Spearman's rank correlation

coefficient r_s . Mean value of r_s was calculated to find the best normalization method for WASPAS.

Method	WASPAS (N1)	WASPAS (N2)	WASPAS (N3)	WASPAS (N4)	WASPAS (N5)	WASPAS (N6)	Ratio system Karande, P. et al.	Reference Point Method Karande, P. et al.
WASPAS (N1)	1	0.7857	0.9642	1	0.75	0.75	0.6071	0.7321
WASPAS (N2)		1	0.75	0.7857	0.2142	0.9642	0.5714	0.6964
WASPAS (N3)			1	0.9642	0.7142	0.7857	0.75	0.7678
WASPAS (N4)				1	0.75	0.75	0.6071	0.7321
WASPAS (N5)					1	0.1785	0.3571	0.375
WASPAS (N6)						1	0.7142	0.7321
Ratio system Karande, P. et al.							1	0.8392
Reference Point Method Karande, P. et al.								1

Table 5: Spearman's rank correlation coefficient r_s between the rankings of MADM methods

Method	WASPAS (N1)	WASPAS (N2)	WASPAS (N3)	WASPAS (N4)	WASPAS (N5)	WASPAS (N6)	Ratio system Karande, P. et al.	Reference Point Method Karande, P. et al.
Mean r_s	0.8236	0.7209	0.8370	0.8236	0.5424	0.7343	0.6808	0.7343

Table 6: Mean Spearman's rank correlation coefficient r_s

VII. CONCLUSIONS

The ranking performance obtained from weighted aggregated sum product assessment (WASPAS) method for different normalization techniques was compared with other MADM methods. Spearman's rank correlation coefficient was used as a measure to evaluate the degree of agreement between the methods. It is evident from Table 6 that normalization technique N5 i.e. Logarithmic Normalization gave the least mean spearman's rank correlation coefficient hence this method is not recommended for the normalization in WASPAS. Normalization method N3 i.e. Linear Normalization (Max-Min) gave the best mean correlation coefficient and can be used as the perfect normalization technique for WASPAS. It can be seen that the criterion for calculating the rank is distinct from each other because while normalizing the decision matrix the performance which is least preferred becomes zero and highly preferred becomes one.

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